# SHREE H.N.SHUKLA INSTITUTE OF PHARMACEUTICAL EDUCATION AND RESEARCH 


B.PHARM
(SEMESTER-I)

# SUBJECT NAME: REMEDIAL MATHEMATICS <br> SUBJECT CODE: BP107TT <br> UNIT 1 

## CHAPTER-2: LOGARITHMS

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## Topic

## Logarithms

\$Definition of logarithm
Properties of logarithm

## \#Common logarithms

## \#Characteristic and Mantissa

\# Worked examples
\$Application of logarithm to solve pharmaceutical problems

## Definition of logarithm

$>$ If $x$ is a real number then its logarithm to the base $a$ is defined as the exponent which when raised to the base of the number $x$ is obtained.

$$
\begin{aligned}
& \log _{a} x=y \\
& x=a^{y} \quad(a>0, a \neq 1, x>0)
\end{aligned}
$$

$>a^{y}=x$ is called exponential form and $\log _{a} x=y$ is called logarithmic form.
$>$ For example;

| Sr. No. | Exponential form | Logarithmic form |
| :---: | :---: | :---: |
| 1 | $3^{4}=81$ | $\log _{3} 81=4$ |
| 2 | $2^{5}=32$ | $\log _{2} 32=5$ |
| 3 | $3^{-2}=\frac{1}{9}$ | $\log _{3}\left(\frac{1}{9}\right)=-2$ |
| 4 | $2^{1}=2$ | $\log _{2} 2=1$ |

## Properties of logarithm

Negative numbers and zero have no logarithms.
$>$ The logarithm of 1 to any base is zero. $\left(\log _{a} 1=0\right)$
$>$ The logarithm of any number $(\neq 1)$ to the same base is unity.

## Laws of logarithm

1) $\log _{a}(m n)=\log _{a} m+\log _{a} n$
2) $\log _{a}\left(\frac{m}{n}\right)=\log _{a} m+\log _{a} n$
3) $\log _{a}\left(m^{n}\right)=n \log _{a} m$
4) $\log _{a}\left(a^{n}\right)=n \log _{a} a=n$

## Common logarithms

The logarithms calculated to base 10 are called common logarithms.
$>$ It is denoted by $\log _{10} a$

## Example-1:

Write the following in logarithmic form.

1) $8^{3}=512 \Rightarrow \log _{8} 512=3$
2) $32 \frac{3}{5}=8 \Rightarrow \log _{32} 8=\frac{3}{5}$
3) $10^{-2}=0.01 \Rightarrow \log _{10} 0.01=-2$
4) $3^{0}=1 \Rightarrow \log _{3} 1=0$
5) $4^{-3}=\frac{1}{64} \Rightarrow \log _{4}\left(\frac{1}{64}\right)=-3$

## Example-2:

Express the following in exponential form.

1) $\log _{9}(6561)=4 \Rightarrow 9^{4}=6561$
2) $\log _{\frac{1}{16}}\left(\frac{1}{8}\right)=\frac{3}{4} \Rightarrow\left(\frac{1}{16}\right)^{3 / 4}=\frac{1}{8}$
3) $\log _{5}\left(\frac{1}{25}\right)=-2 \Rightarrow 5^{-2}=\frac{1}{25}$
4) $\log _{21} 1=0 \Rightarrow 21^{0}=1$

## Example-3:

Simplify the following terms;

1) $\log 15-\log 5-\log 2$
2) $\frac{1}{2} \log 49-3 \log 2+\frac{1}{3} \log 27$
3) $\log 3 x+3 \log x$
4) $4 \log 5+2 \log 4$

## Solution:

1) $\log 15-\log 5-\log 2=\log 15-(\log 5+\log 2)$

$$
\begin{aligned}
& =\log 15-\log (5 \times 2) \\
& =\log 15-\log 10 \\
& =\log \left(\frac{15}{10}\right) \\
& =\log \left(\frac{3}{2}\right)
\end{aligned}
$$

2) $\frac{1}{2} \log 49-3 \log 2+\frac{1}{3} \log 27=\log (49)^{1 / 2}-\log 2^{3}+\log (27)^{1 / 3}$

$$
\begin{aligned}
& =\log \left(7^{2}\right)^{1 / 2}-\log 8+\log \left(3^{3}\right)^{1 / 3} \\
& =\log 7-\log 8+\log 3 \\
& =(\log 7+\log 3)-\log 8 \\
& =\log (7 \times 3)-\log 8 \\
& =\log \left(\frac{21}{8}\right)
\end{aligned}
$$

3) $\log 3 x+3 \log x=\log 3 x+\log x^{3}$

$$
\begin{aligned}
& =\log \left(3 x \cdot x^{3}\right) \\
& =\log \left(3 x^{4}\right)
\end{aligned}
$$

4) $4 \log 5+2 \log 4=\log 5^{4}+\log 4^{2}$

$$
\begin{aligned}
& =\log 625+\log 16 \\
& =\log (625 \times 16) \\
& =\log (10000) \\
& =\log 10^{4} \\
& =4 \log 10 \\
& =4
\end{aligned}
$$

## Example-4:

Find the values of $x$ in each of the following:

1) $\log _{2} x=4$
2) $\log _{x} 64=6$
3) $\log _{10} x=-2$

## Solution:

1) $\log _{2} x=4 \Rightarrow 2^{4}=x \Rightarrow x=2 \times 2 \times 2 \times 2=16$
2) $\log _{x} 64=6 \Rightarrow x^{6}=64 \Rightarrow x^{6}=2 \times 2 \times 2 \times 2 \times 2 \times 2=x^{6}=2^{6} \Rightarrow x=2$
3) $\log _{10} x=-2 \Rightarrow x=10^{-2} \Rightarrow x=\frac{1}{10^{2}} \Rightarrow x=0.01$

## Example-5:

Prove that

1) $\log \frac{11}{5}+\log \frac{14}{3}-\log \frac{22}{15}=\log 7$
2) $3 \log 4+2 \log 5-\frac{1}{3} \log 64-\frac{1}{2} \log 16=2$

## Solution:

1) LHS $=\left(\log \frac{11}{5}+\log \frac{14}{3}\right)-\log \frac{22}{15}$
$=\log \left(\frac{11}{5} \times \frac{14}{3}\right)-\log \frac{22}{15}$
$=\log \left[\frac{\frac{11}{5} \times \frac{14}{3}}{\frac{22}{15}}\right]$

$$
\begin{aligned}
& =\log \left(\frac{15 \times 11 \times 14}{5 \times 3 \times 22}\right) \\
& =\log 7=R H S
\end{aligned}
$$

$\therefore \log \frac{11}{5}+\log \frac{14}{3}-\log \frac{22}{15}=\log 7$
2) $L H S=3 \log 4+2 \log 5-\frac{1}{3} \log 64-\frac{1}{2} \log 16$

$$
\begin{aligned}
& =\log 4^{3}+\log 5^{2}-\log (64)^{1 / 3}-\log (16)^{1 / 2} \\
& =\log 64+\log 25-\log \left(4^{3}\right)^{1 / 3}-\log \left(4^{2}\right)^{1 / 2} \\
& =\log (64 \times 25)-\log 4-\log 4 \\
& =\log (64 \times 25)-2 \log 4 \\
& =\log (64 \times 25)-\log 4^{2} \\
& =\log (64 \times 25)-\log 16 \\
& =\log \left(\frac{64 \times 25}{16}\right) \\
& =\log 100 \\
& =\log 10^{2} \\
& =2 \log 10 \\
& =2=R H S
\end{aligned}
$$

## Some standard forms of Decimal and Exponential

| Sr. No. | Log form | Exponential form |
| :--- | :---: | :---: |
| 1 | $\log _{10} 1=0$ | $10^{0}=1$ |
| 2 | $\log _{10} 10=1$ | $10^{1}=10$ |
| 3 | $\log _{10} 100=2$ | $10^{2}=100$ |
| 4 | $\log _{10} 0.1=-1$ | $10^{-1}=\frac{1}{10}=0.1$ |
| 5 | $\log _{10} 0.01=-2$ | $10^{-2}=\frac{1}{100}=0.01$ |

## Characteristic and Mantissa of a logarithm

$\Rightarrow$ Consider $n$ be a positive real number and let $n=m \times 10^{p}$ be the standard form, where $p$ is an integer and $m$ is a real number between 1 and 10 .
i.e. $1 \leq m<10$
$>$ We have,

$$
\begin{align*}
& n=m \times 10^{p} \\
& \therefore \log n=\log \left(m \times 10^{p}\right)=\log m+\log 10^{p}=\log m+p \log 10 \\
& \therefore \log n=\log m+p \quad \ldots \ldots \ldots \ldots(1) \tag{1}
\end{align*}
$$

$>$ Since $p$ is an integer and $1 \leq m<10$
Now,

$$
1 \leq m<10 \Rightarrow \log 1 \leq \log m<\log 10 \Rightarrow 0 \leq \log m<1
$$

$>$ Thus, the logarithm of positive real number $n$ consists of two parts:
i) The integral part $(p)$, which is an integer.
ii) The decimal part $(\log m)$, which lies between 0 and 1 .
> Therefore, the integral part is known as the Characteristic and the decimal part is known as Mantissa.
$>$ So, from the equation (1), we have

$$
\begin{gathered}
\log n=p+\log m=\text { integral part }+ \text { decimal part } \\
=\text { Characteristic }+ \text { Mantissa }
\end{gathered}
$$

## Method to find Characteristic

Method-1: To find the characteristic of a negative number ( $n<1$ )
Step-1: Let $n$ be the given number
Step-2: Write the number in the standard form $\left(n=m \times 10^{p}\right)$ of decimal
Step-3: The index of 10 in the standard form, that means $p$ is the Characteristic of given number
Method-2: To find the characteristic of a positive number ( $n \geq 1$ )
Step-1: Let $n$ be the given number
Step-2: Write the number in the standard form $\left(n=m \times 10^{p}\right)$ of decimal
Step-3: If the number is graeater than or equal to 1 , then obtain the Characteristic by using the formula
Characteristic $=($ number of digit to the left of the decimal point $)-1$

## Example-6:

Obtain the Characteristic of the logarithms of each of the following numbers by using their standard forms.
a) 2123.50
b) 134.02
c) 75.1330
d) 2.1444
e) 0.39139
f) 0.06213
g) 0.00712
h) 0.00069
i) 0.00003

## Solution:

| Sr. No. | Number | Standard form | Characteristic |
| :---: | :---: | :---: | :---: |
| a) | 2123.50 | $2.12350 \times 10^{3}$ | 3 |
| b) | 134.02 | $1.3402 \times 10^{2}$ | 2 |
| c) | 75.1330 | $7.51330 \times 10^{1}$ | 1 |
| d) | 2.1444 | $2.1444 \times 10^{0}$ | 0 |
| e) | 0.39139 | $3.9139 \times 10^{-1}$ | -1 |
| f) | 0.06213 | $6.213 \times 10^{-2}$ | -2 |
| g) | 0.00712 | $7.12 \times 10^{-3}$ | -3 |
| h) | 0.00069 | $6.9 \times 10^{-4}$ | -4 |
| i) | 0.00003 | $3.0 \times 10^{-5}$ | -5 |

## Mantissa of a logarithm of a number

$>$ The table of logarithm is used to find the mantissa of logarithm of numbers. (A table of logarithm is appended at the end of the material)
$>$ Table consists of 90 rows and 20 columns.
$>$ In a table, every row begin with two digit number like as $10,11,12,13,14$, $\ldots . . . . . . . . . . . . . . .97,98,99$ and every column is headed by single digit number $0,1,2, \ldots \ldots \ldots \ldots \ldots .8,9$.
$>$ On the right of the table, we have big column, which is divided into 9subcolumns headed by the digits $1,2,3 \ldots \ldots \ldots . .8,9$. This column is called the column of mean differences.

## Note:

$>$ If the given number has one digit, we replace it by a two digit number obtained by adjoining zero to the right side of the given number. For example, the number of 3 is to be replaced by 30 for getting the mantissa.
$>$ The digits used to obtain the mantissa of a given number are called the significant digits.

## Method to find Mantissa of a logarithm of a number

Step-1: Let $n$ be given number
Step-2: Write the significant digits of a given number
Step-3: Select the first two digit, in the significant digit
Step-4: Look in the row starting with the number, obtained in Step-3 in the logarithm table
Step-5: After getting row in Step-4, look at the number in the number column headed by zero
Step-6: If there is fourth significant digit, then move to the column of mean difference and look under the column headed by the fourth significant digit. Now, find the number there and add this number to number obtained in Step-5. Then, we get the required mantissa of a given number. Otherwise, the number getting in Step-5 is the required mantissa.

## Example-7:

Obtain the mantissa of the logarithm of the number 1974

## Solution:

We have $\log 1974=n$
First, we look the row starting with 19.
In this row, look at the number in the column headed by 7 .
This number is (2945).
Now, move to the column of mean differences and look under the column headed by 4 in the row corresponding to 19 .
We get the number (9) there.
Here, we add these number as $2945+9=2954$ which is the required mantissa of $\log 1974$.

## Example-8:

Calculate the mantissa of the logarithm of the number 74.21

## Solution:

We have $\log 74.21=n$
First, we look the row starting with 74.
In this row, look at the number in the column headed by 2.
This number is (8704).
Now, move to the column of mean differences and look under the column headed by 1 in the row corresponding to 74 .
We get the number (1) there.
Here, we add these number as $8704+1=8705$ which is the required mantissa of $\log (74.21)$.

## Method to find complete value of $\log n$

Step-1: Let the given number be $n$
Step-2: Obtain the characteristic
Step-3: Obtain the mantissa
Step-4: The required result is $\log n=$ characterisic + mantissa

## Example-9:

Use logarithm table, to calculate the value of the following:
a) $\log (0.00073615)$
b) $\log (2.0017)$
c) $\log (106.0606)$
d) $\log (20.201)$

## Solution:

a) Let $n=0.00073615$

We have the first four non-zero digit is 7361
Now, the Characteristic of $n$ is -4 and Mantissa of $n$ is 8670
So, $\log (0.00073615)=-4+0.8670=4.8670$
b) Let $n=2.0017$

We have the first four non-zero digit is 2001
Now, the Characteristic of $n$ is 0 and Mantissa of $n$ is 3012
So, $\log (2.0017)=0+0.3012=0.3012$
c) Let $n=106.0606$

We have the first four non-zero digit is 1060
Now, the Characteristic of $n$ is 2 and Mantissa of $n$ is 0235
So, $\log (106.0606)=2+0.0253=2.0253$
d) Let $n=20.201$

We have the first four non-zero digit is 2020
Now, the Characteristic of $n$ is 1 and Mantissa of $n$ is 3054
So, $\log (20.201)=1+0.3054=1.3054$

## Application of logarithm to solve Pharmaceutical problems

1) Glomerular filtration rate (GFR)

The normal range for GFR is $1.25-2.10 \mathrm{~m}=1.25-2.10 \mathrm{~m}^{2} / \mathrm{s}=1.73 \mathrm{~m}^{2}$ and varies with sex and age.
$>$ The basic formula for clearance $\left(C l_{x}\right)$ of a substance X is
$C l_{x}=\frac{U_{x} \cdot V}{P_{x}}$
Where, $U_{x}=$ Urine concentration of X
$\mathrm{V}=$ Urine volume per time
$P_{x}=$ Plasma concentration of X

Taking log of equation (1), we get

$$
\log C l_{x}=\log \left(\frac{U_{x} \cdot V}{P_{x}}\right)=\log U_{x}+\log V-\log P_{x}=A(\text { says })
$$

$>$ Now, taking antilog, we get the value of $\left(C l_{x}\right)$

$$
C l_{x}=\operatorname{antilog}(A)
$$

2) First order kinetics
$>$ The change in drug concentration based on time can be expressed as
$C=C_{0} \cdot e^{-k t}$
Where, $\mathrm{C}=$ concentration at time t
$C_{0}=$ initial concentration
$\mathrm{k}=$ rate constant
$\mathrm{t}=$ time
$\mathrm{e}=$ natural logarithm
Taking logarithm, we get

$$
\begin{aligned}
& \log C=\log \left(C_{0} \cdot e^{-k t}\right) \\
& \quad=\log C_{0}+\log e^{-k}=\log \mathrm{C}_{0}-\mathrm{kt} \log \mathrm{e}=\log \mathrm{C}_{0}-\mathrm{kt}(0.43429)
\end{aligned}
$$

3) Drug-concentration capacity-limit process
$>$ We have,

$$
\log C=\log C_{0}+\frac{\left(C_{0}-C\right)}{2.303 K_{m}}-\frac{V_{\max }}{2.303 K_{m}}
$$

Where, $\mathrm{C}=$ drug concentration
$K_{m}=$ Michaelis-Menten constant
$V_{\max }=$ Theoretical maximum rate of the process

LOGARITHMS TABLES

|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 123 | 456 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $1 \cdot 0$ | . 0000 | 0043 | 0086 | 0128 | 0170 | 0212 | 0253 | 0294 | 0334 | 0374 | 4812 | 172125 | 293337 |
|  | -0414 | 0453 0828 | 0492 0864 | 0531 0899 | 0569 | 0607 | 0645 | 0682 | 0719 | 0755 | 4811 | 151923 | 263034 |
| 1.2 | $\cdot 0792$ .1139 | 0828 1173 | 0864 1206 | 0899 1239 | 0934 | 0969 | 1004 | 1038 | 1072 | 1106 | 3710 | 141721 | $24 \quad 2831$ |
| 1.3 | -1139 | 1173 | 1206 | 1239 | 1271 | 1303 | 1335 | 1367 | 1399 | 1430 | 3610 | 131619 | $\begin{array}{llll}23 & 26 & 29\end{array}$ |
| 1.4 | -1461 | 1492 | 1523 | 1553 | 1584 | 1614 | 1644 | 1673 | 1703 | 1732 | 369 | 121518 | 212427 |
| 1.6 | - 2 | 179 | 1818 | 1847 | 1875 | 1903 | 1931 | 1959 | 1987 | 2014 | 368 | 111417 | 2022.25 |
| 1.6 | -2 | 206 | 2095 | 2122 | 2148 | 2175 | 2201 | 2227 | 2253 | 2279 | $\begin{array}{lll}3 & 5 & 8\end{array}$ | 111316 | 182124 |
| 1.7 | . 2304 | 2330 | 2355 | 2380 2625 | 2405 | 2430 | 2455 | 2480 | 2504 | 2529 | 25 | 101215 | 172022 |
| 1.9 | - 2788 | 2810 | 2833 | 2856 | 2648 | 2672 | 2695 | 2718 | 2742 | 2765 | 25 | 91214 | 161921. |
|  |  |  |  |  |  |  |  |  |  | 2989 | 7 | 91113 | 161820 |
| 2.0 | -3010 | 3032 | 3054 | 3075 | 3096 | 3118 | 3139 | 3160 | 3181 | 3201 | 246 | 81113 | 151719 |
| $2 \cdot 2$ | - 3222 | 3243 | 3263 | 3284 | 3304 | 3324 | 3345 | 3365 | 3385 | 3404 |  |  |  |
| 2.2 2.3 | - 3424 | 344 | 3464 | 3483 | 3502 | 3522 | 3541 | 3560 | 3379 | 3404 <br> 3598 | $\begin{array}{lll}2 & 4 & 6 \\ 2 & 4 & 6\end{array}$ | 81012 | 7 |
|  |  | 3636 | 36 | 3674 | 3692 | 3711 | 3729 | 3747 | 3766 | 3784 | $\begin{array}{lll}2 & 4 & 6 \\ 2 & 6\end{array}$ | $\begin{array}{rrrr}8 & 10 \\ 7 & 9 & 11\end{array}$ | $\begin{array}{llll}14 & 15 & 17 \\ 13 & 15 & 17\end{array}$ |
| 2.4 2.5 | -3802 -3979 | 3820 3997 | 3838 4014 | 3856 | 3874 | 3892 | 3909 | 3927 | 3945 | 3962 | 245 | 7911 | 6 |
| 2.6 | - 4150 | 4166 | 4 | 4031 | 4048 | 4065 | 4082 | 4099 | 4116 | 4133 | $\begin{array}{llll}2 & 3 & 5\end{array}$ | $7 \quad 910$ | 121416 |
|  |  |  |  |  |  | 4232 | 4249 | 4265 | 4281 | 4298 | 235 | 7810 | $\begin{array}{llll}11 & 13 & 15\end{array}$ |
| 2.7 2.8 | .4314 .4472 | 4330 | 4346 | 4362 | 4378 | 4393 | 4409 | 4425 | 4440 | 4456 | 23 | 9 | 4 |
| 2.9 | -4624 | 4639 | 4654 | 4518 | 4533 | 4548 | 4564 | 4579 | 4594 | 4609 | $\begin{array}{llll}2 & 3 & 5\end{array}$ | 6 6 889 | $\begin{array}{lll}11 & 13 & 14 \\ 11 & 12\end{array}$ |
|  |  |  |  |  |  | 46 | 4713 | 4728 | 4742 |  | 3.4 | $\begin{array}{lll}6 & 7 & 9\end{array}$ | 101213 |
| 3.0 | 4 | 4786 | 4800 | 4814 | 4829 | 4843 | 4857 | 4871 | 4886 | 4900 | 134 | $\begin{array}{llll}6 & 7 & 9\end{array}$ | 101113 |
| $3 \cdot 1$ | - 4914 | 4928 | 4942 | 4955 | 4969 | 4983 | 4997 | 5011 |  |  |  |  |  |
| $3 \cdot 2$ | - 5051 | 5065 | 5079 | 5092 | 5105 | 5119 | 5132 | 5145 | 5024 5159 | 5038 5172 5302 | $\begin{array}{lll}1 & 3 & 4 \\ 1 & 3 & 4 \\ 1\end{array}$ | $\begin{array}{lll}6 & 7 & 8 \\ 5 & 7 & 8\end{array}$ | 101112 |
| $3 \cdot 3$ | - 5185 | 5198 | 5211 | 5224 | 5237 | 5250 | 5263 | 5276 | 5289 | 5302 | 13 | $\begin{array}{lll} 5 & 7 & 8 \\ 5 & 6 & 8 \end{array}$ | $\begin{array}{lll} 9 & 11 & 12 \\ 9 & 10 & 12 \end{array}$ |
| 3.5 | . 5315 | 5328 | 5340 | 5353 | 5366 | 5378 |  |  |  |  |  |  |  |
| $3 \cdot 5$ | . 5451 | 5453 5575 | 5465 | 5478 | 5490 | 5502 | 5514 | 5403 | 5416 5539 | 5428 | $1 \begin{aligned} & 13 \\ & 1\end{aligned}$ |  | 1011 |
|  | - 5 | 5575 | 5587 | 5599 | 5611 | 5623 | 5635 | 5647 | 5658 | 5670 | $\begin{array}{lll}1 & 2 & 4\end{array}$ | $\begin{array}{lll}5 & 6 & 7\end{array}$ | $\begin{array}{llll}9 & 10 & 11 \\ 8 & 10 & 11\end{array}$ |
| 3.7 | - 5682 | 5694 | 5705 | 5717 | 5729 | 5740 | 5752 | 5763 | 5775 | 5786 |  |  |  |
| $3 \cdot 8$ | - 5798 | 580 | 5821 | 5832 | 5843 | 5855 | 5866 | 5877 | 5888 | 5899 | 123 | $\begin{array}{lll}5 & 6 & 7 \\ 5 & 6 & 7\end{array}$ | 910 |
|  |  |  | 5933 | 5944 | 5955 | 5966 | 5977 | 5988 | 5999 | 6010 | 12.3 | $\begin{array}{llll}4 & 5 & 7\end{array}$ | 8 8 8 910 |
| 4.0 | -6021 | 6031 | 6042 | 6053 | 6064 | 6075 | 6085 | 6096 | 6107 | 6117 | 123 | 4556 | 8910 |
| 4.1 | -6128 | 6138 | 6149 | 6160 | 6170 | 6180 | 6191 | 6201 | 6212 | 6222 | 2 |  | 788 |
| $4 \cdot 3$ | -6232 | 6243 | 6253. | 6263 | 6274 | 6284 | 6294 | 6304 | 6314 | 6325 | 12 | 4.436 | 7 |
| $4 \cdot 3$ | -6335 | 6345 | 6355 | 6365 | 6375 | 6385 | 6395 | 6405 | 6415 | 6425 | 123 | 4456 | 7 <br> 7 8 |
| 4.4 | -6435 | $64$ | 6454 | 6464 | 6474 | 6484 | 6493 | 6503 | 6513 | 6522 | 123 | 456 | 789 |
| 4.6 | . 6628 | 6637 | 6646 | 6656 | 6571 6665 | 6580 6675 | 6590 | 6 | 66 | 6618 | 123 | 6 | $\begin{array}{lll}7 & 8 & 9\end{array}$ |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 4.8 | . 6812 | 6821 | 6739 6830 | 6839 | 6848 | 6767 6857 | 6776 | 6785 6875 | 6794 | $6803$ | $\begin{array}{lll}1 & 2 & 3 \\ 1 & 2 & 3\end{array}$ | 5 | 678 |
| 4 | -6902 | 6911 | 6920 | 6928 | 6937 | 6946 | 6955 | 6964 | 6972 | 6981 | 123 | 45 | $\begin{array}{llll}6 & 7 & 8\end{array}$ |
| 5. | . 6990 | 6998 | 7007 | 7016 | 702 | 7033 | 7042 | 7050 | 7059 | 7067 | 123 | 345 | 678 |
| 5 | - 7076 | 7084 | 7093 | 7101 | 7110 | 7118 | 7126 | 7135 | 7143 | 7152 | 123 | $\begin{array}{llll}3 & 4 & 5\end{array}$ | 678 |
| 5 | .7160 | 7168 | 7177 | 7185 | 7193 | 7202 | 7210 | 7218 | 7226 | 7235 | 122 | 4 | $\begin{array}{lll}6 & 7 & 8\end{array}$ |
| 5.3 5.4 | .7243 .7324 | 7332 | 7259 7340 | 72 |  | 728 | 7292 | 7300 | 7308 | 7316 | 122 | $\begin{array}{llll}3 & 4 & 5\end{array}$ | 6 |
|  |  |  |  |  |  |  |  |  | 738 |  | 122 | $\begin{array}{llll}3 & 4 & 5\end{array}$ | 7 |

LOGARITHMS TABLES (Contd.)


